

Y13 Chapter 1-3 Quiz

TIP: draw a clear diagram for each situation.

1. A person on a frictionless trolley shoots water horizontally from a fire extinguisher. The combined mass of the person, fire extinguisher and trolley is 100kg. The diameter of the nozzle is 1cm. 5 litres of water flows out in 10 seconds. What is the acceleration of the person on the trolley?

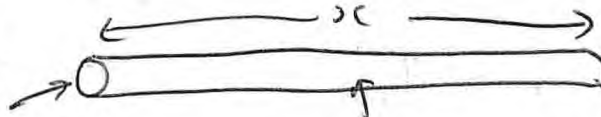
$$a = \frac{F}{m} \quad F = \frac{\Delta p}{\Delta t} = v \frac{\Delta m}{\Delta t}$$

I know that 1 litre of water has $m = 1 \text{ kg}$

$$\frac{\Delta m}{\Delta t} = \frac{5 \text{ kg}}{10 \text{ s}} = 0.5 \text{ kg s}^{-1}$$

in 1 second

$$\text{area is } \pi \times 0.5^2$$



Volume is 5000 cm^3

$$x \times \text{area} = \text{volume} \quad \therefore x = \frac{5000 \text{ cm}^3}{\pi \times 0.5^2} = 6336 \text{ cm} \quad \underline{63.36 \text{ m/s}}$$

so water goes 636 cm in 1 sec.

$$\therefore v = 6.36 \text{ m/s} \quad F = 6.36 \times 0.5 = 3.18 \text{ N} \quad a = \frac{3.18 \text{ N}}{100 \text{ kg}} = 0.032 \text{ m/s}^2$$

2. A spring has a spring constant of $k = 100 \text{ N/m}$ and an original length of 10 cm . The spring is compressed between two frictionless trolleys until its length is 2 cm . Trolley A has a mass of 500 g and trolley B has a mass of 1000 g . The trolleys are released from rest. Find the speed that each trolley moves off at.

$$\text{Energy in spring} = \frac{1}{2} k (\Delta L)^2$$

$$\Delta L = 8 \text{ cm} = 0.08 \text{ m} \quad \therefore E = \frac{1}{2} \times 100 \times (0.08)^2 = 0.32 \text{ J}$$

initial momentum is zero so final momentum is zero.

$$m_A v_A = -m_B v_B \quad 500 v_A = -1000 v_B \quad v_A = -2 v_B$$

must conserve energy.

$$\frac{1}{2} m_A v_A^2 + \frac{1}{2} m_B v_B^2 = 0.32 \text{ J} \quad m_A v_A^2 + m_B v_B^2 = 0.64 \text{ J}$$

$$0.5 \text{ kg} \times v_A^2 + 1 \text{ kg} \times v_B^2 = 0.64 \text{ J} \quad \therefore v_A^2 + 2 v_B^2 = 1.28$$

$$v_A^2 + 2(-2v_B)^2 = 1.28 \quad 6v_B^2 = 1.28 \quad v_B = 0.46 \text{ m/s}^{-1} \\ v_A = 0.92 \text{ m/s}^{-1}$$

3. a) A 1kg mass is connected to a piece of copper wire with circular cross-section that is 1m long. The yield stress of copper is 70MPa. The wire is attached to a strong support so that the weight hangs vertically down.

What is the minimum diameter of the wire so that the copper does not yield?

$$\sigma = F/A \quad A = F/\sigma \quad A = \pi r^2$$

$$\pi r^2 = F/\sigma \quad r^2 = \frac{F}{\sigma \pi} \quad r = \sqrt{\frac{F}{\sigma \pi}}$$

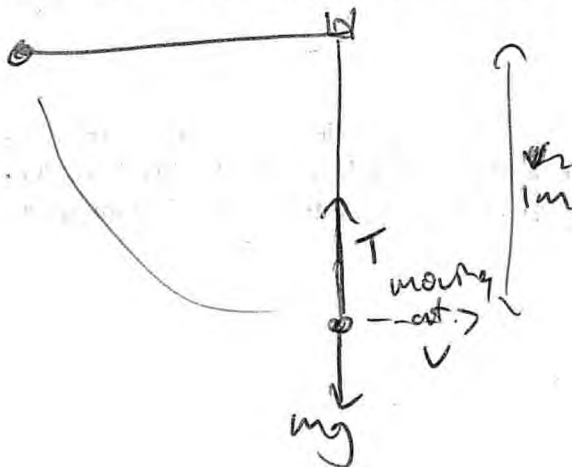
$$d = 2r = 2 \sqrt{\frac{F}{\sigma \pi}} = 2 \sqrt{\frac{1 \times 9.81}{70 \times 10^6 \times \pi}}$$

$$= 422 \times 10^{-4} \text{ m}$$

$$= 0.42 \text{ mm}$$

- b) The weight is then lifted up and to the side so that the wire is horizontal. The weight is released and swings in a circular arc.

What is the minimum diameter of the wire so that the copper does not yield now?



at bottom of swing,

$$\frac{1}{2} m v^2 = mgh$$

$$\frac{1}{2} v^2 = gh$$

$$v^2 = 2gh$$

circular motion:

$$F = T - mg = \frac{mv^2}{r} \quad v^2 = 2gh$$

$$\text{so } T - mg = \frac{m \times 2gh}{r} \quad r = h \quad \text{so } T - mg = 2mg$$

$$T = 3mg = \text{3 times } T \text{ in part A}$$

\therefore area must be 3x larger so diameter must be

$$\sqrt{3} \times \text{larger so } \sqrt{3} \times 0.42 = 0.73 \text{ mm}$$